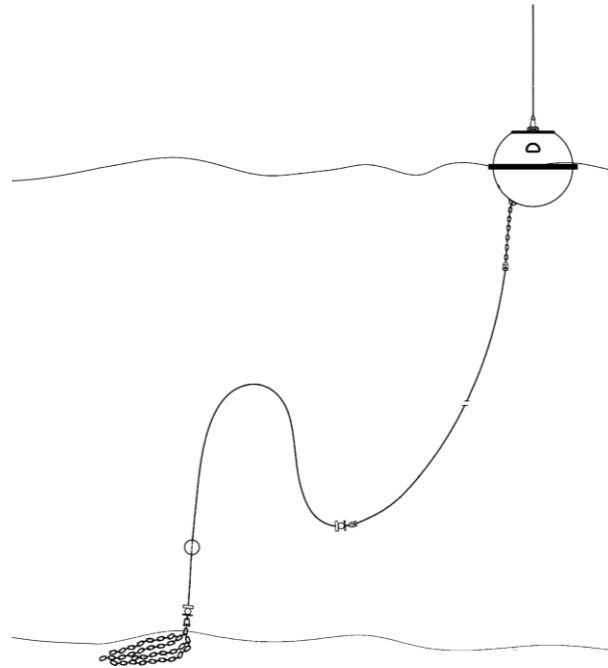


Lagrangian Measurement of Waves by Buoys

Mark L. McAllister and Ton S. van den Bremer

2nd International Workshop on Waves, Storm Surges and Coastal Hazards - Melbourne

11th November 2019



Lagrangian Measurement of Waves by Buoys

- Motivation
- Second-Order Motion of a Wave-Following Measurement Buoy
- Statistical Properties of Directionally Spread Ocean Waves Measured by Buoys
- Approximate retrospective correction method for crest heights





Photo credit: CDIP



Photo credit: CDIP

Motivation

Chair: Val Swail

A1 *Quantifying Wave Measurement Differences in Historical and Present Wave Buoy Systems*

8:50 a.m. R.E. Jensen, V. Swail, R.H. Bouchard and B. Bradshaw

Presenter: Jensen [Download Presentation](#)

A2 *Field Evaluation of the Wave Module for NDBC's New Self-Contained Ocean Observing Payload (SCOOP) on Modified NDBC Hulls*

9:10 a.m. Richard Bouchard, Rodney R. Riley, Lex A. LeBlanc, Michael Vasquez, Michael Robbie, Robert E. Jensen, Mary A. Bryant and Laura A. Fiorentino

Presenter: Bouchard [Download Presentation](#)

A3 *Correcting for Changes in the NDBC Wave Records of the United States*

9:30 a.m. Elizabeth A. Livermont, Jon K. Miller and Thomas O. Herrington

Presenter: Livermont [Download Presentation](#)

9:50 a.m. Break

Session B: Wave Measurement - 2

Chair: Robert Jensen

B1 *Data Buoy Cooperation Panel (DBCP) Task Team on Wave Measurement (TT-WM)*

10:30 a.m. Val Swail and Robert Jensen

Presenter: Swail [Download Presentation](#)

B2 *Open Ocean Storm Waves in the Arctic*

10:50 a.m. Takuji Waseda, Adrean Webb, Kazutoshi Sato, Jun Inoue, Alison Kohout, Bill Penrose and Scott Penrose

Presenter: Waseda [Download Presentation](#)

B3 *A project of concrete stabilized spar buoy for monitoring near-shore environment*

11:10 a.m. Sergei I. Badulin, Vladislav V. Vershinin, Andrey G. Zatsepin, Dmitry V. Ivonin, Dmitry G. Levchenko, Alexander G. Ostrovskii and Leopold I. Lobkovsky

Presenter: Badulin [Download Presentation](#)

B4 *Measuring the 'First Five' with HF radar*

11:30 a.m. Lucy R Wyatt

Presenter: Wyatt [Download Presentation](#)

B5 *The use and limitations of satellite remote sensing for the measurement of wind speed and wave height*

11:50 a.m. Ian Young

Presenter: Young [Download Presentation](#)

12:10 p.m. Lunch

Session C: Wave Design Criteria

Chair: Andrew Cox

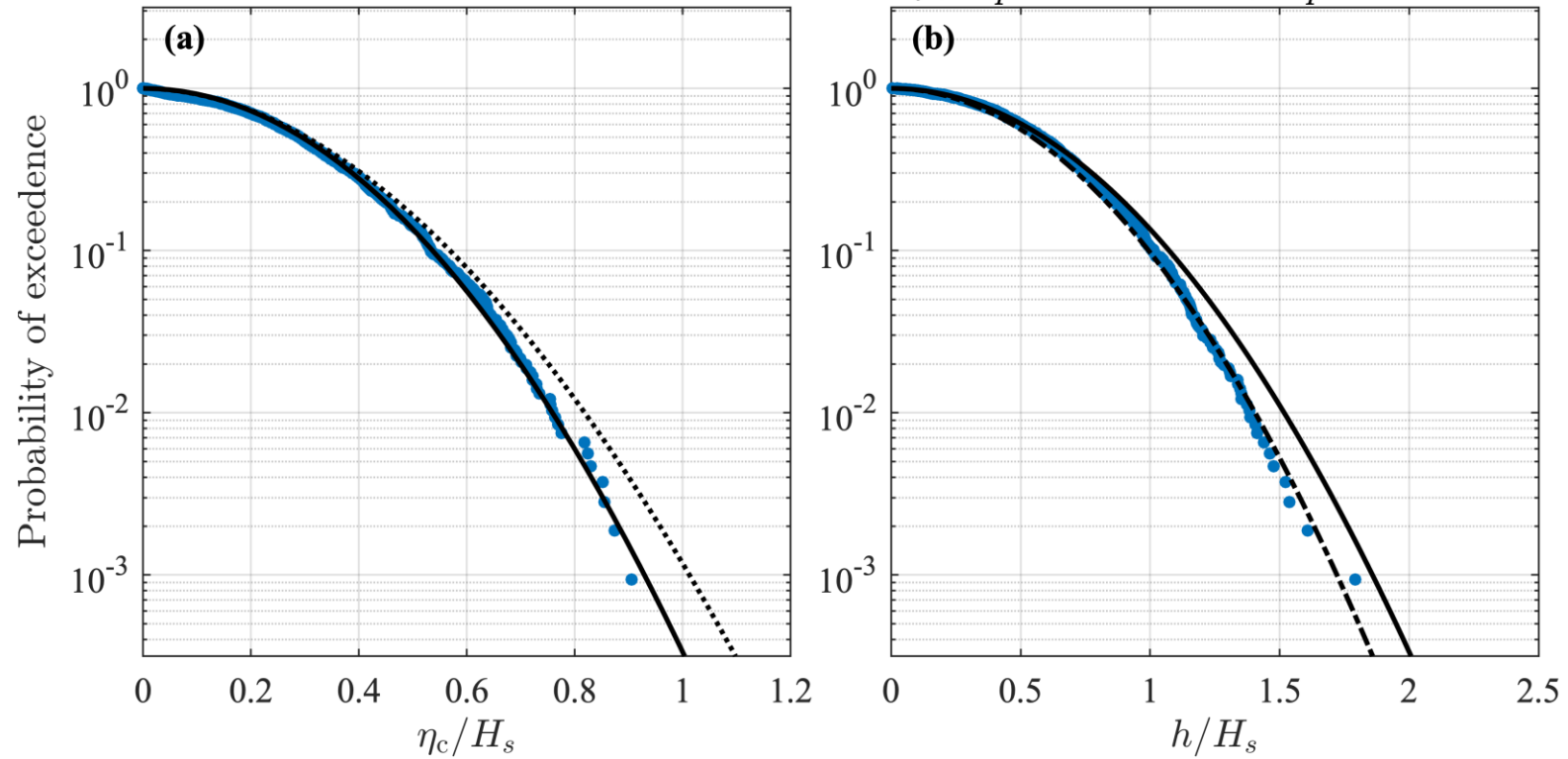
C1 *Individual Wave Height and Wave Crest Distributions - Full Scale Measurements - North Sea*

1:30 p.m. Børge Kvingedal

Presenter: Kvingedal [Download Presentation](#)

Motivation

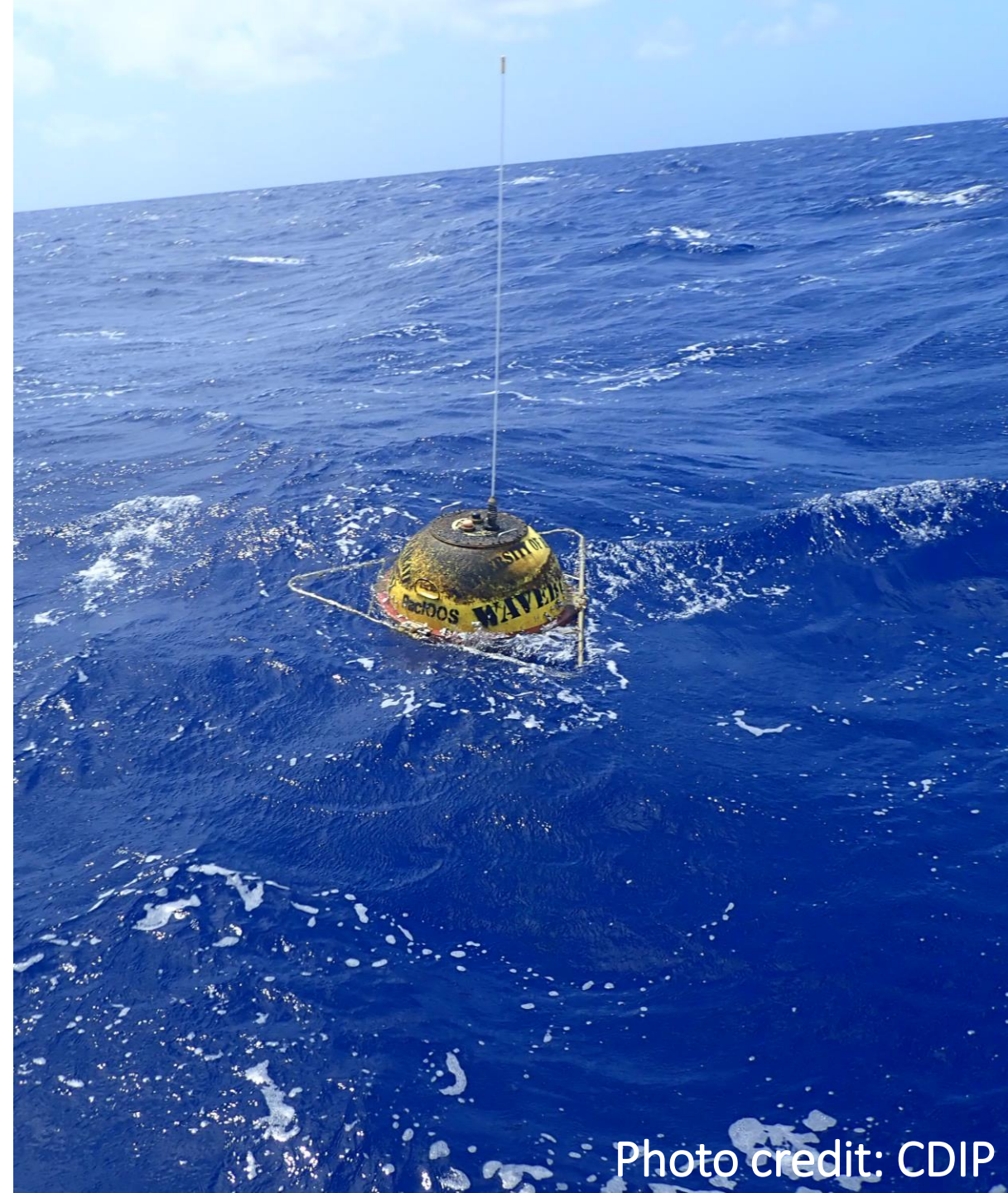
San Nicholas Island CDIP buoy, $k_p H_s \approx 0.25$, $k_p d \approx 10$



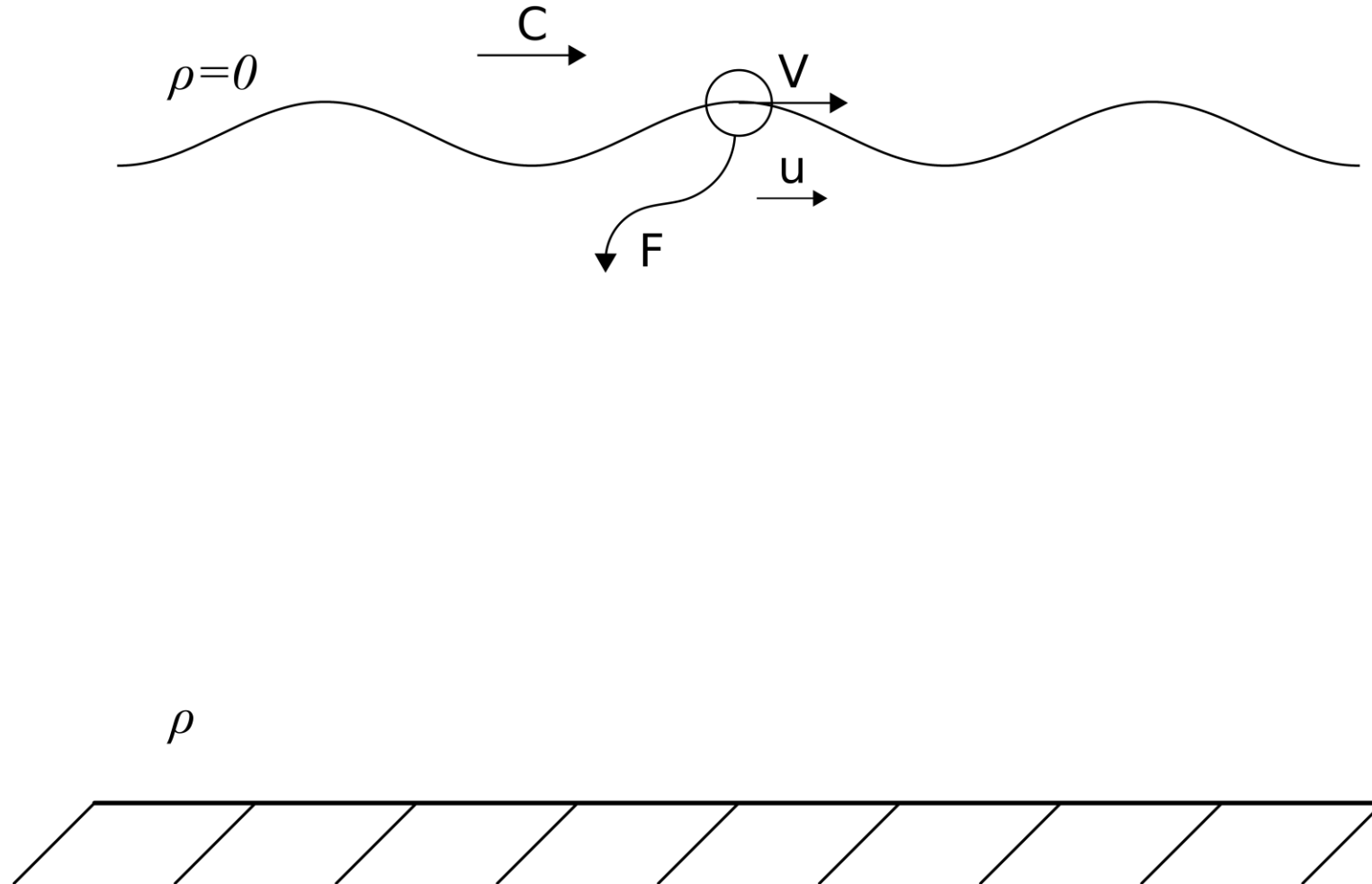
- Buoy Data
- Rayleigh
- Farristall (2000)
- - - - Tayfun & Fedele (2007)

Motivation

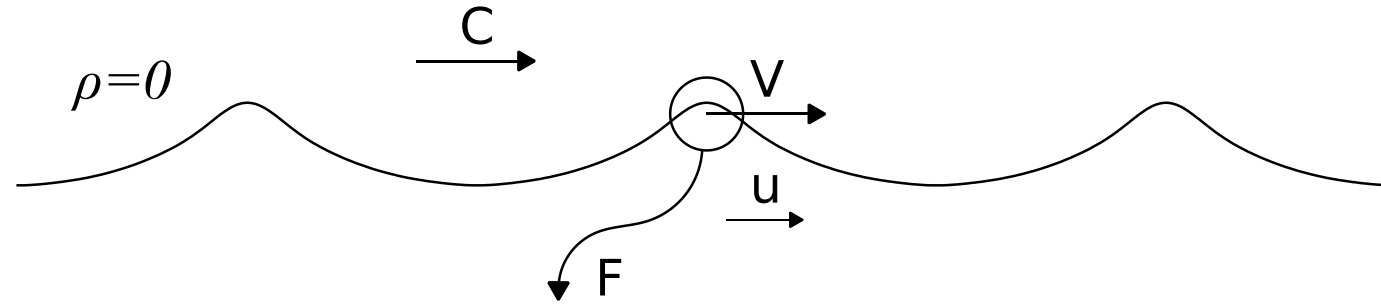
- Buoys avoid large crest
- Lack of mooring compliance drags buoys under crests
- Low sampling rate misses crests
- Lagrangian motion “linearises” crests
- Instrumentation and signal processing



Second-Order Motion of a Wave-Following Measurement Buoy

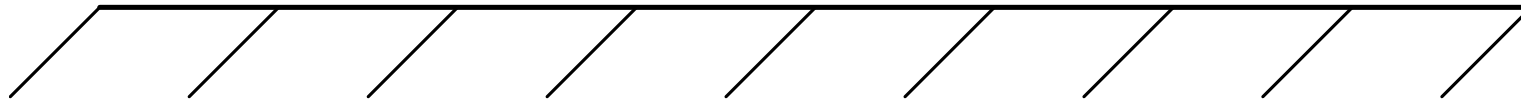


Second-Order Motion of a Wave-Following Measurement Buoy

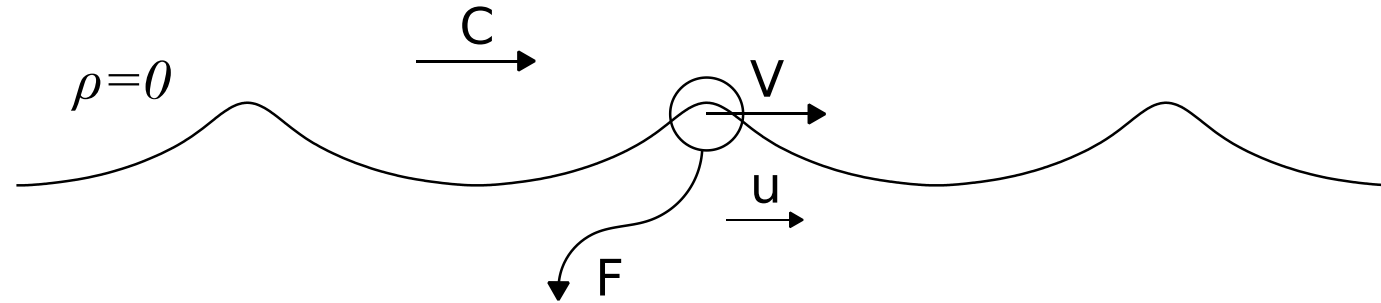


$$\eta_E = \eta_E^{(1)} + \eta_E^{(2)} + O(3)$$

ρ



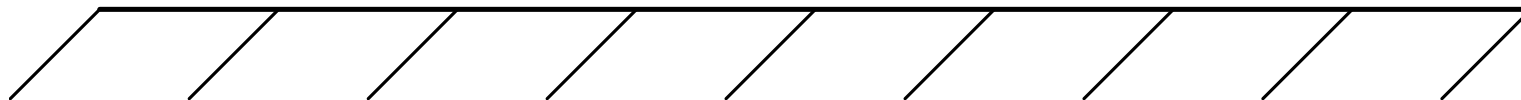
Second-Order Motion of a Wave-Following Measurement Buoy



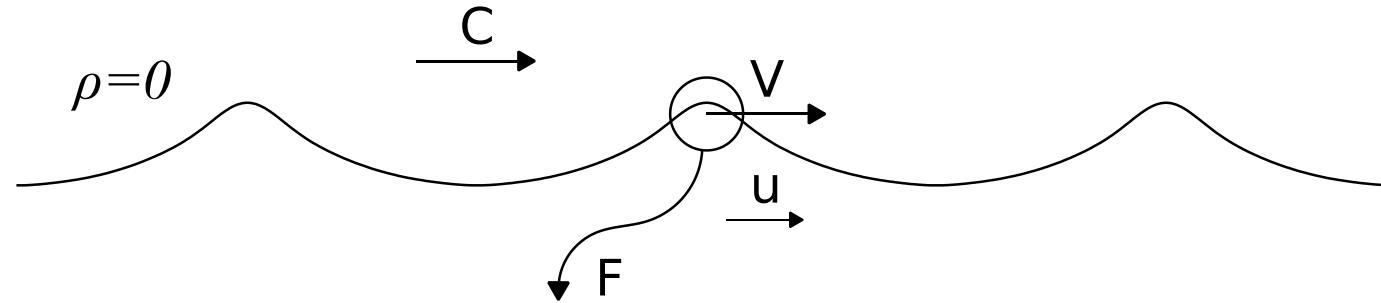
$$\eta_E = \eta_E^{(1)} + \eta_E^{(2)} + O(3)$$

$$\eta_L^{(2)} = \eta_E^{(2)} + \Delta\eta_L^{(2)}$$

ρ



Second-Order Motion of a Wave-Following Measurement Buoy

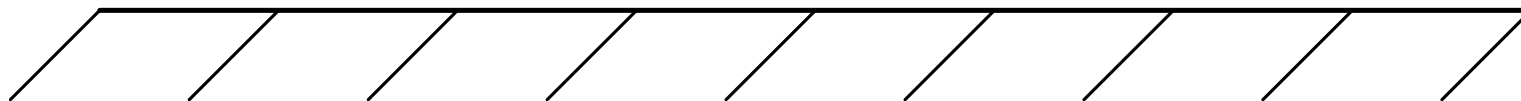


$$\eta_E = \eta_E^{(1)} + \eta_E^{(2)} + O(3)$$

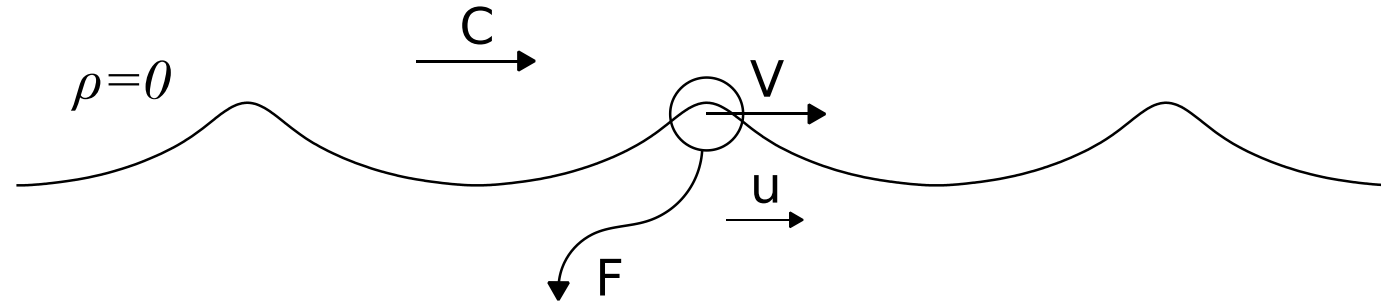
$$\eta_L^{(2)} = \eta_E^{(2)} + \Delta\eta_L^{(2)}$$

$$\Delta\eta_L^{(1)} = \Delta x_H^{(1)} \cdot \nabla_H \eta^{(1)}$$

ρ



Second-Order Motion of a Wave-Following Measurement Buoy



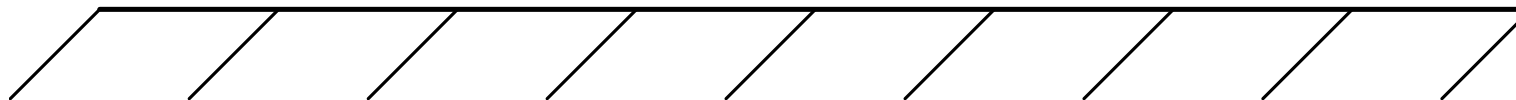
$$\eta_E = \eta_E^{(1)} + \eta_E^{(2)} + O(3)$$

$$\eta_L^{(2)} = \eta_E^{(2)} + \Delta\eta_L^{(2)}$$

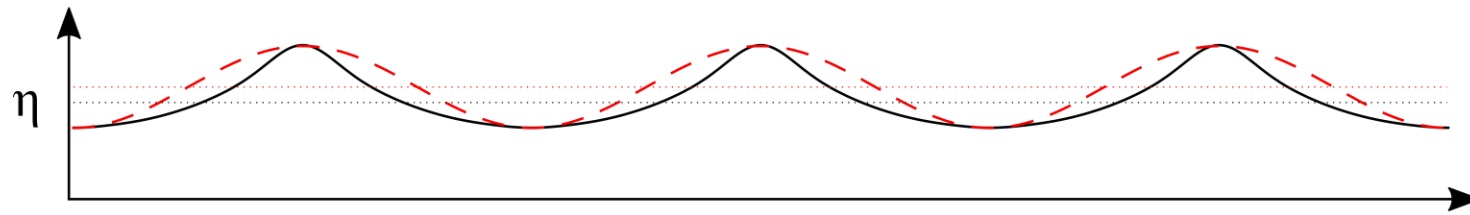
$$\Delta\eta_L^{(1)} = \Delta x_H^{(1)} \cdot \nabla_H \eta^{(1)}$$

$$\eta_E^{(2)} = -\Delta\eta_L^{(2)} \text{ (Deep water)}$$

ρ



Second-Order Motion of a Wave-Following Measurement Buoy



$$\text{Eulerian } \eta = \text{———}$$

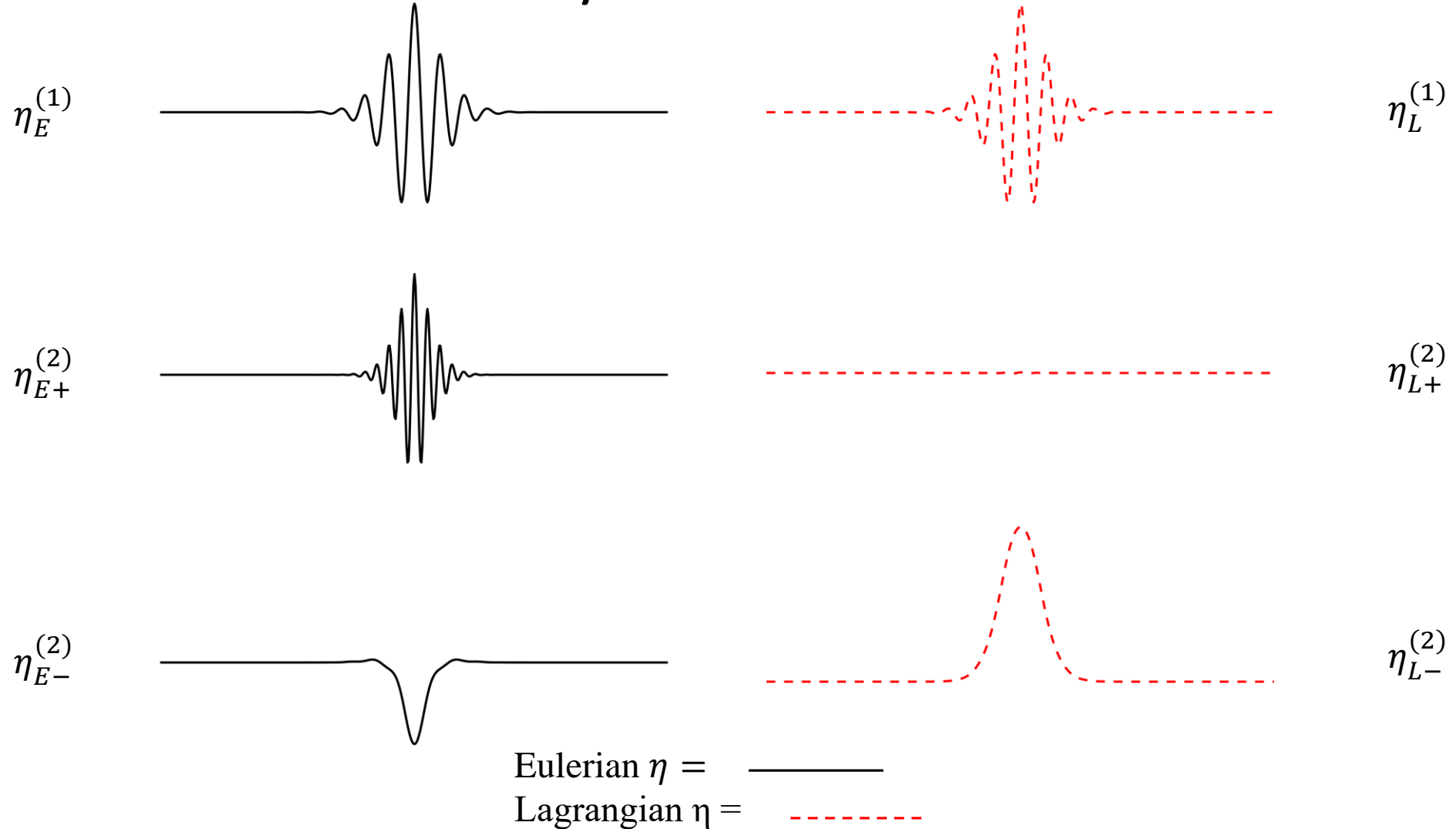
$$\text{Lagrangian } \eta = \text{-----}$$

$$\eta_L^{(2)} = \eta_E^{(2)} + \Delta\eta_L^{(2)}$$

$$\Delta\eta_L^{(1)} = \Delta x_H^{(1)} \cdot \nabla_H \eta^{(1)}$$

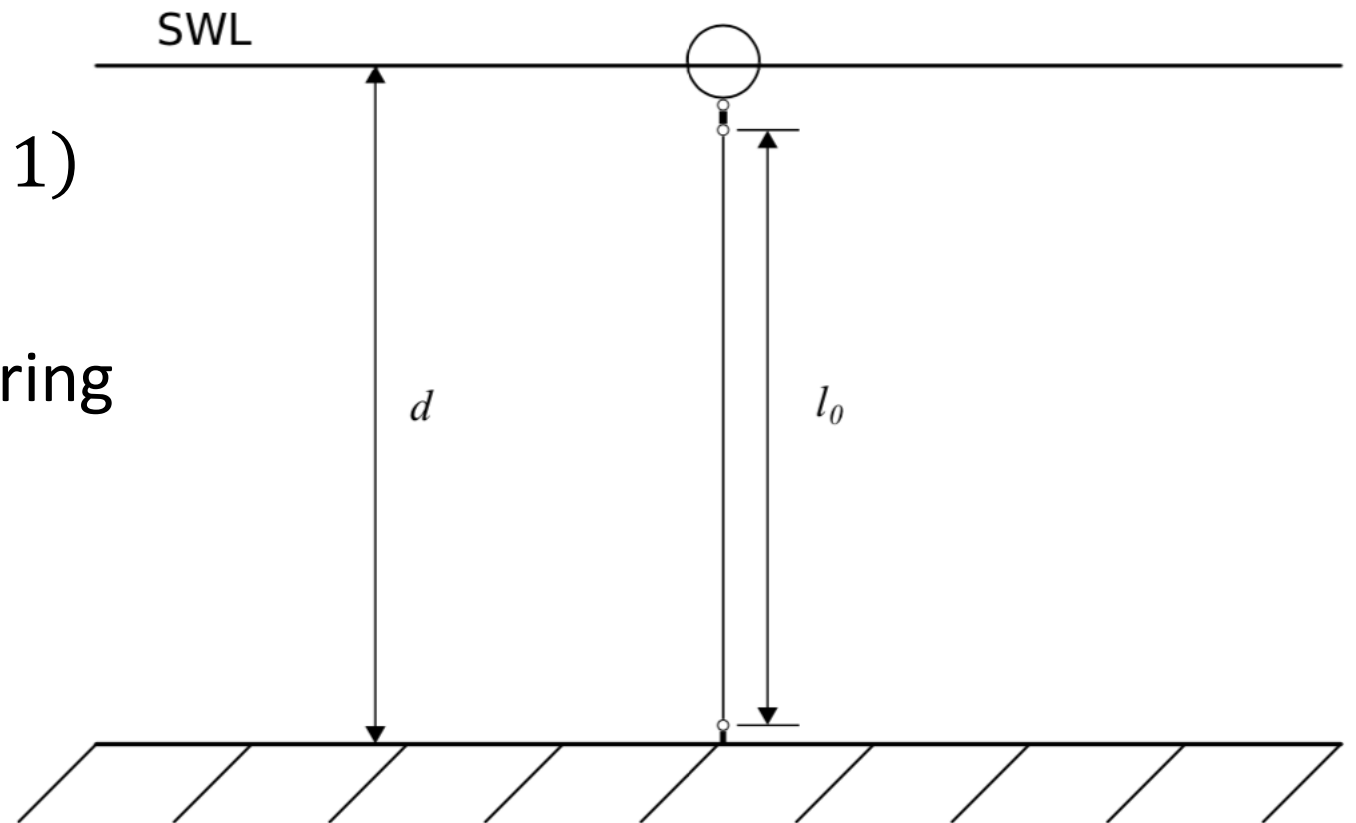
$$\eta_E^{(2)} = -\Delta\eta_L^{(2)} \text{ (Deep water)}$$

Second-Order Motion of a Wave-Following Measurement Buoy



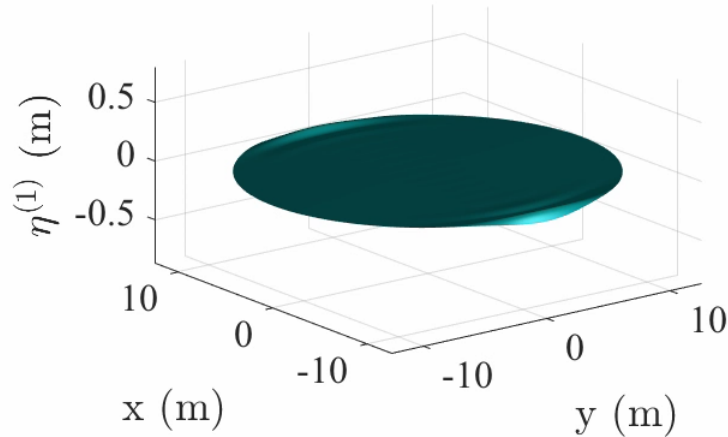
Second-Order Motion of a Wave-Following Measurement Buoy

- Diameter 0.07m ($D/\lambda_0 \ll 1$)
- Density $\approx 0.5\rho_w$
- Highly-flexible taught mooring
- Depth 2 m ($k_0 d = 3 - 4$)
- Wave amplitude ≈ 0.2 m
($k_0 a_0 / k_p H_s \approx 0.3$)

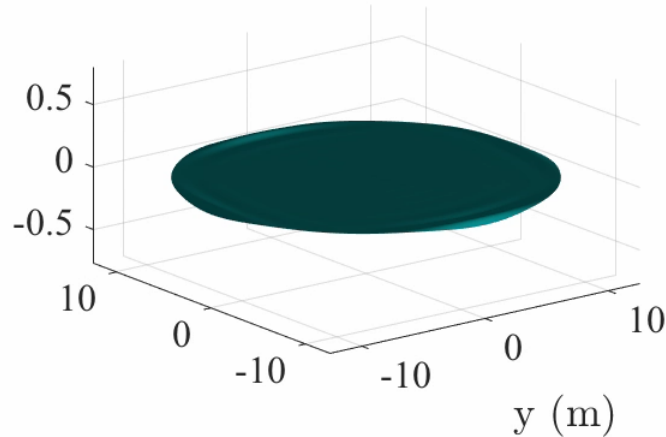


Second-Order Motion of a Wave-Following Measurement Buoy

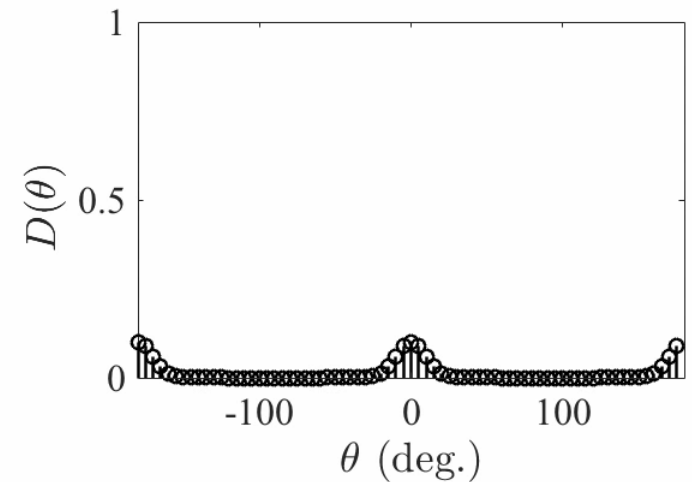
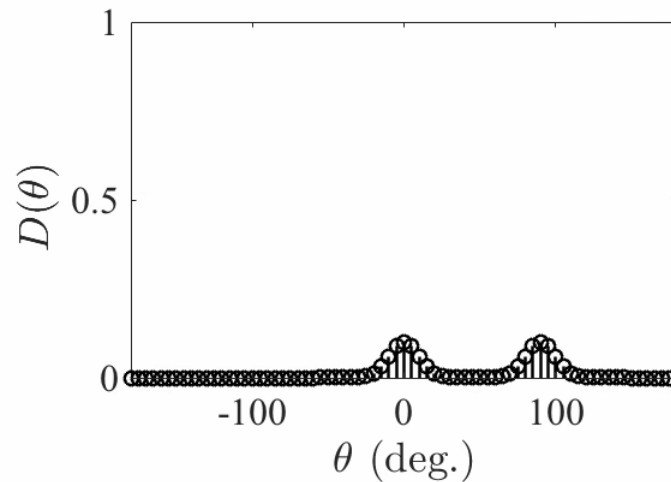
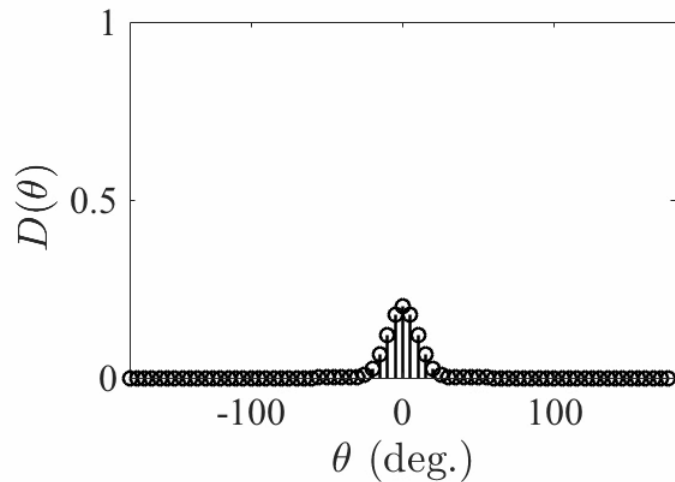
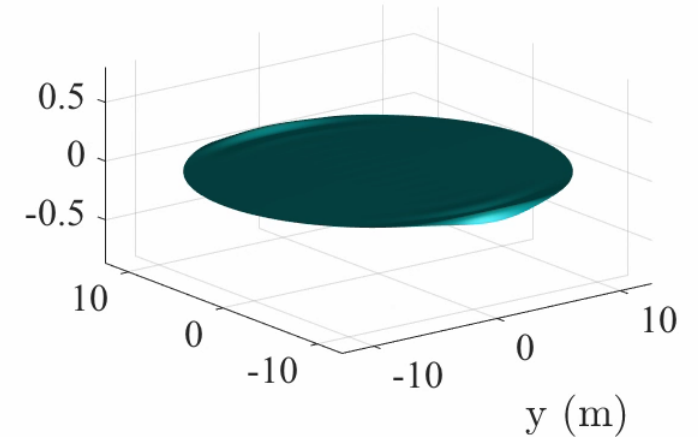
$\sigma_\theta = 10^\circ, \Delta\theta = 0^\circ$



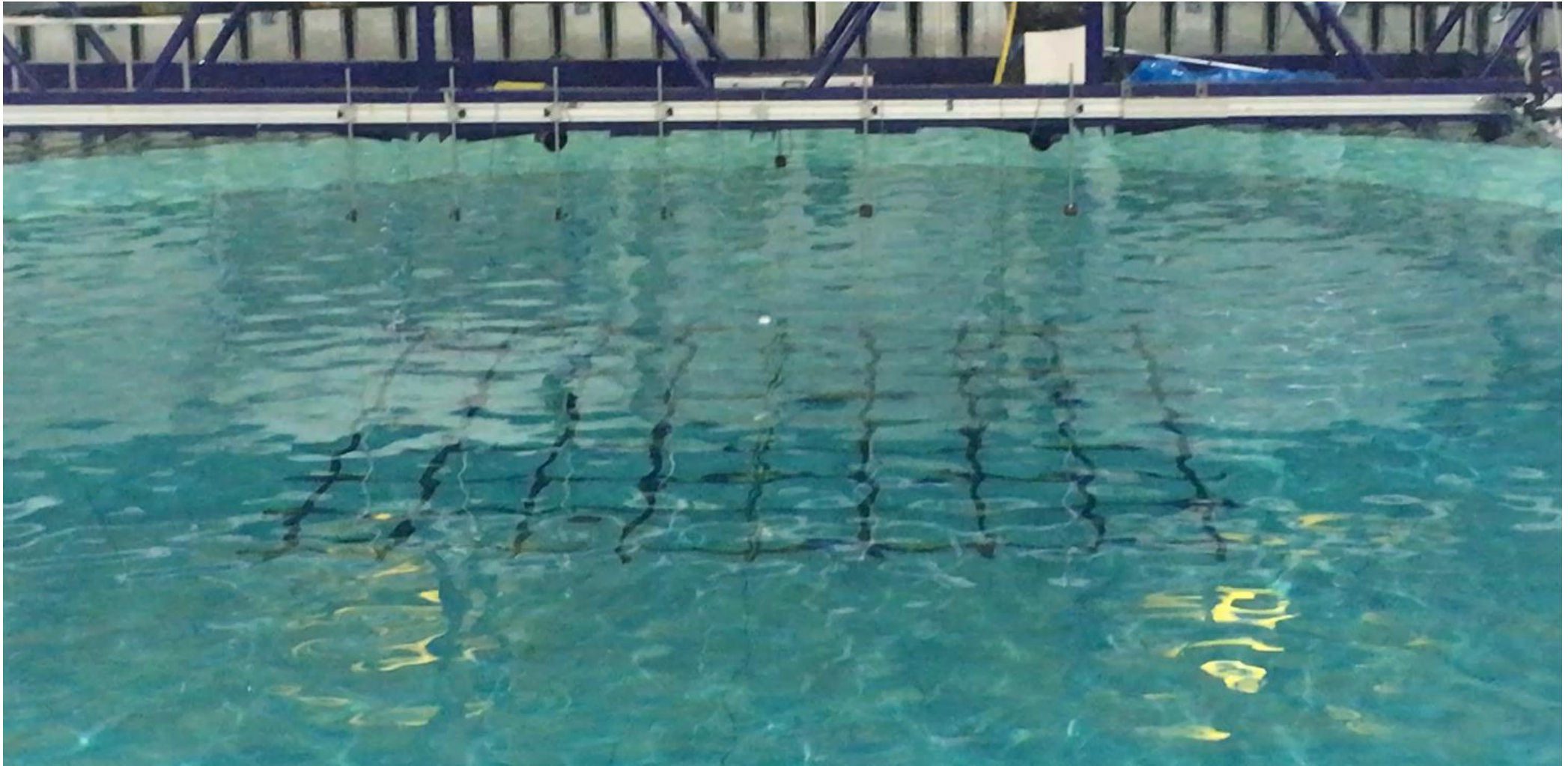
$\sigma_\theta = 10^\circ, \Delta\theta = 90^\circ$



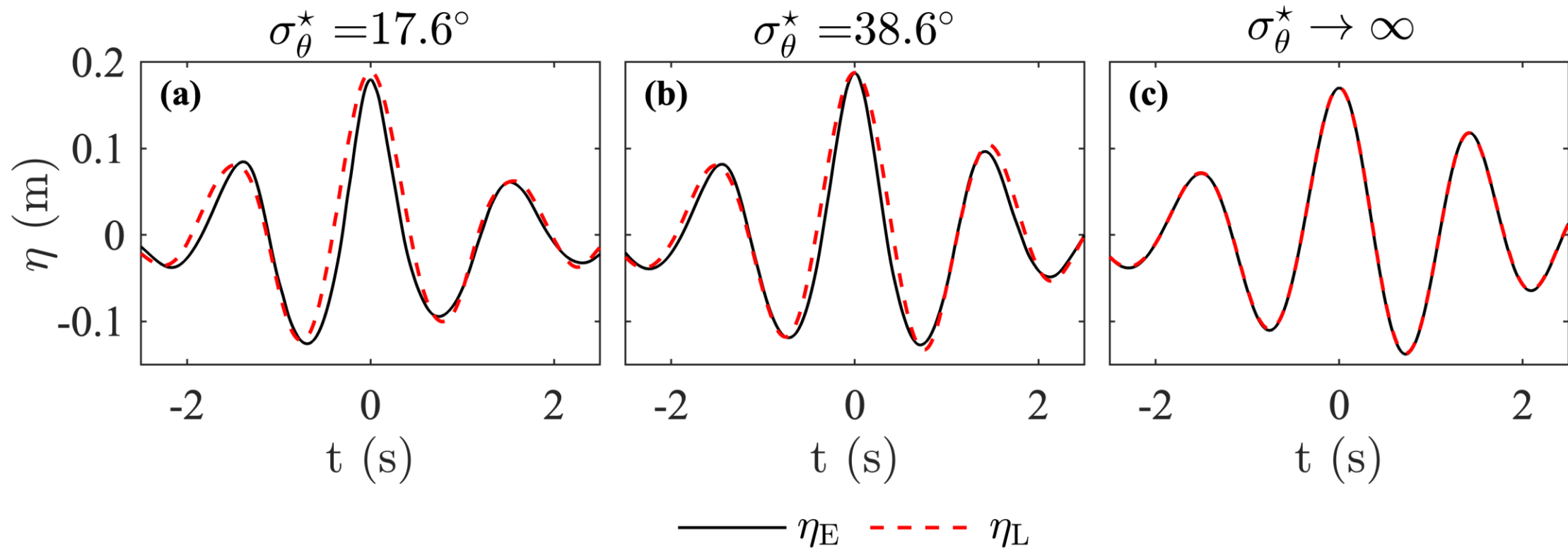
$\sigma_\theta = 10^\circ, \Delta\theta = 180^\circ$



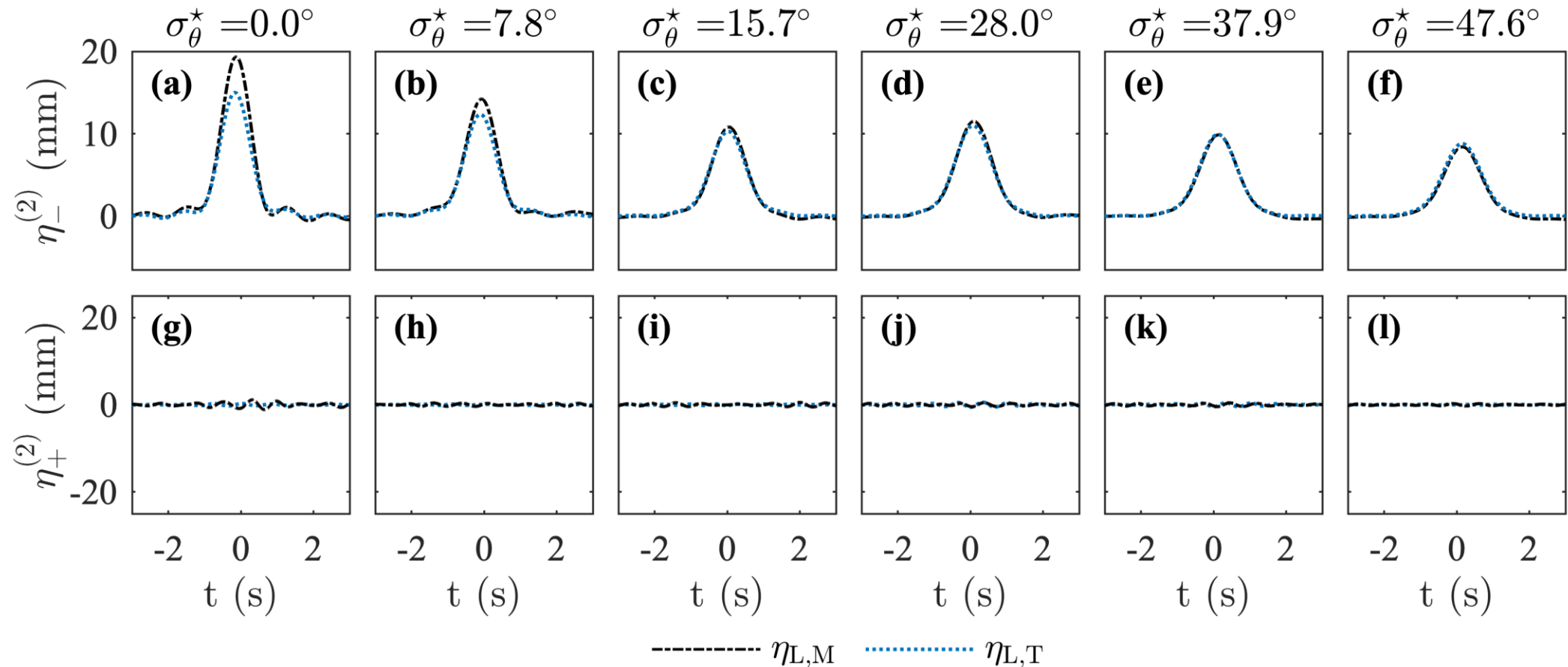
Second-Order Motion of a Wave-Following Measurement Buoy



Second-Order Motion of a Wave-Following Measurement Buoy

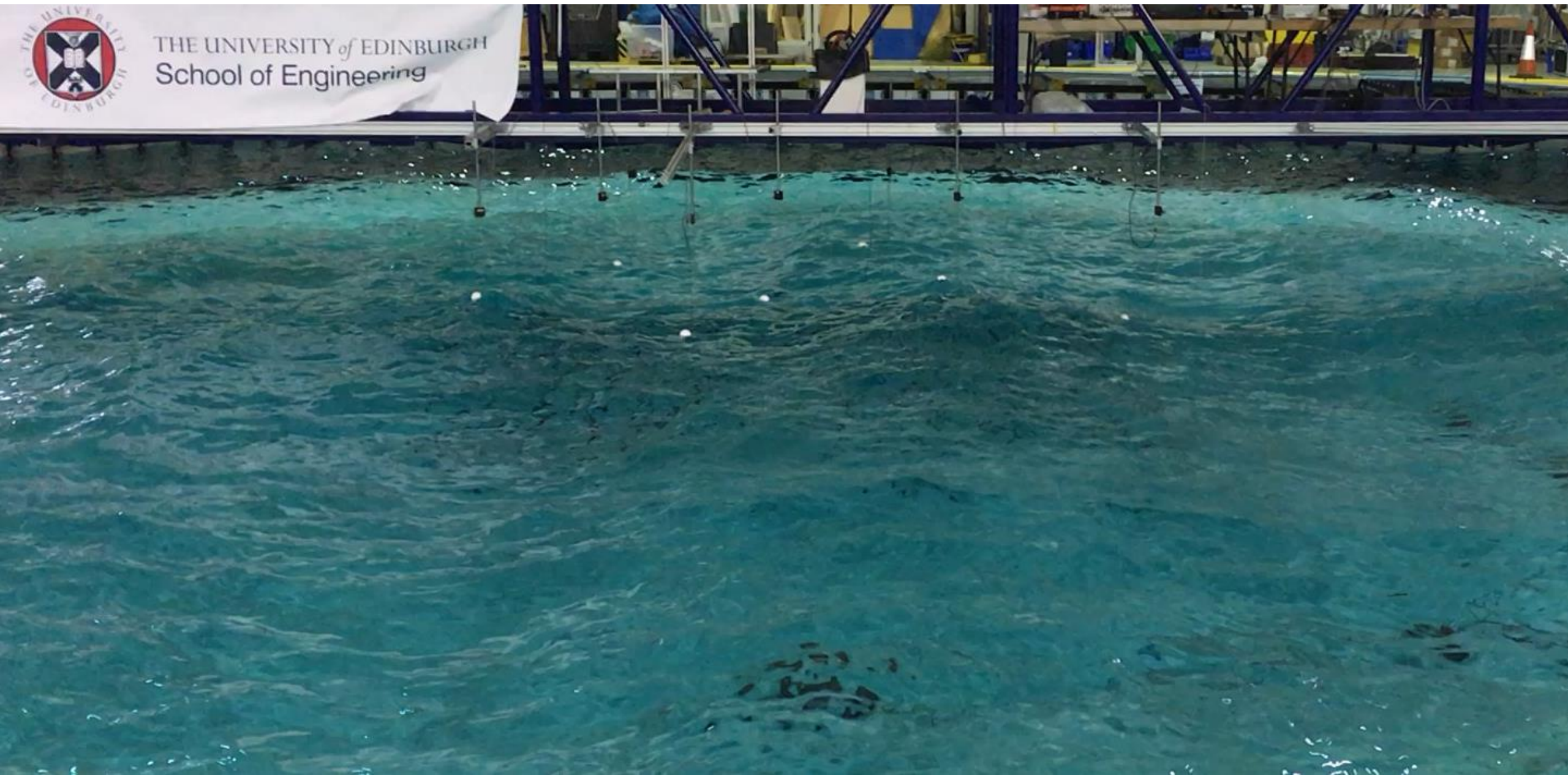


Second-Order Motion of a Wave-Following Measurement Buoy

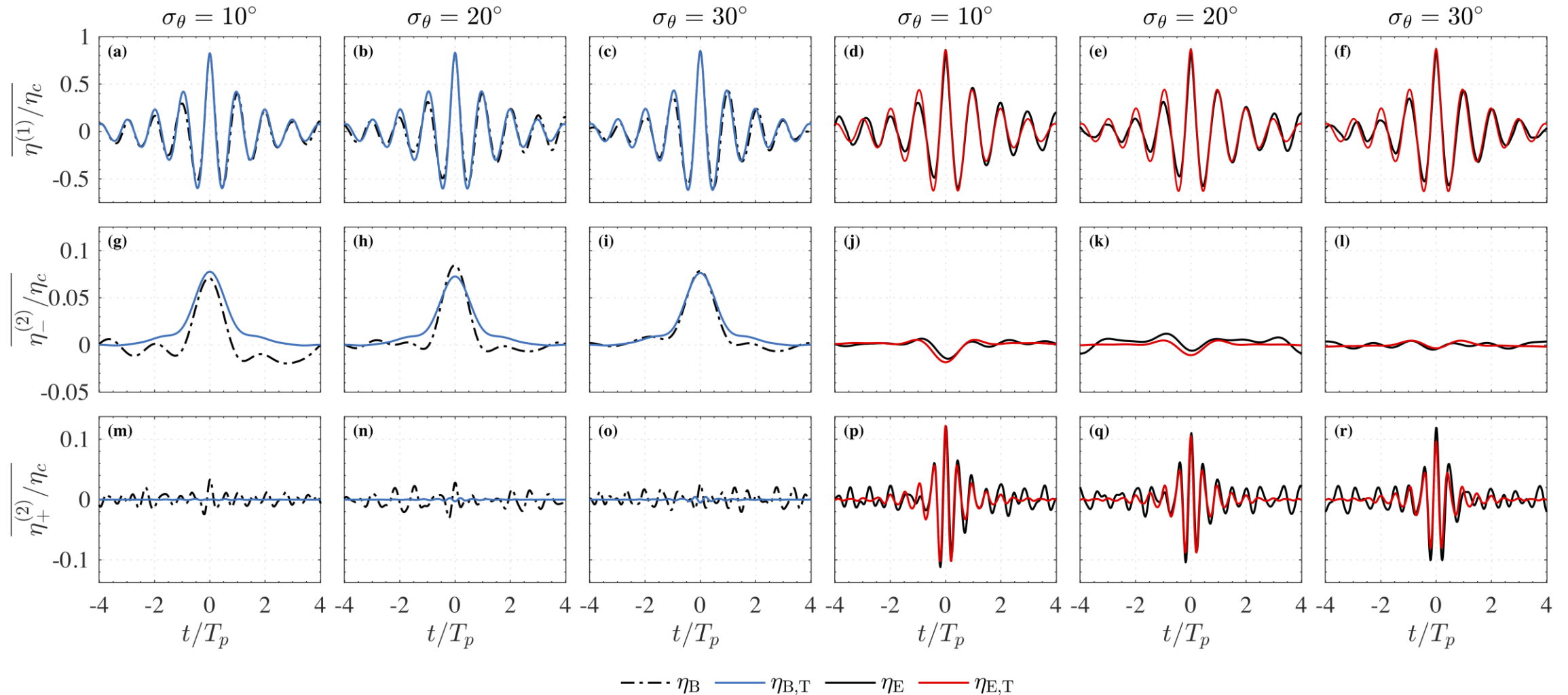




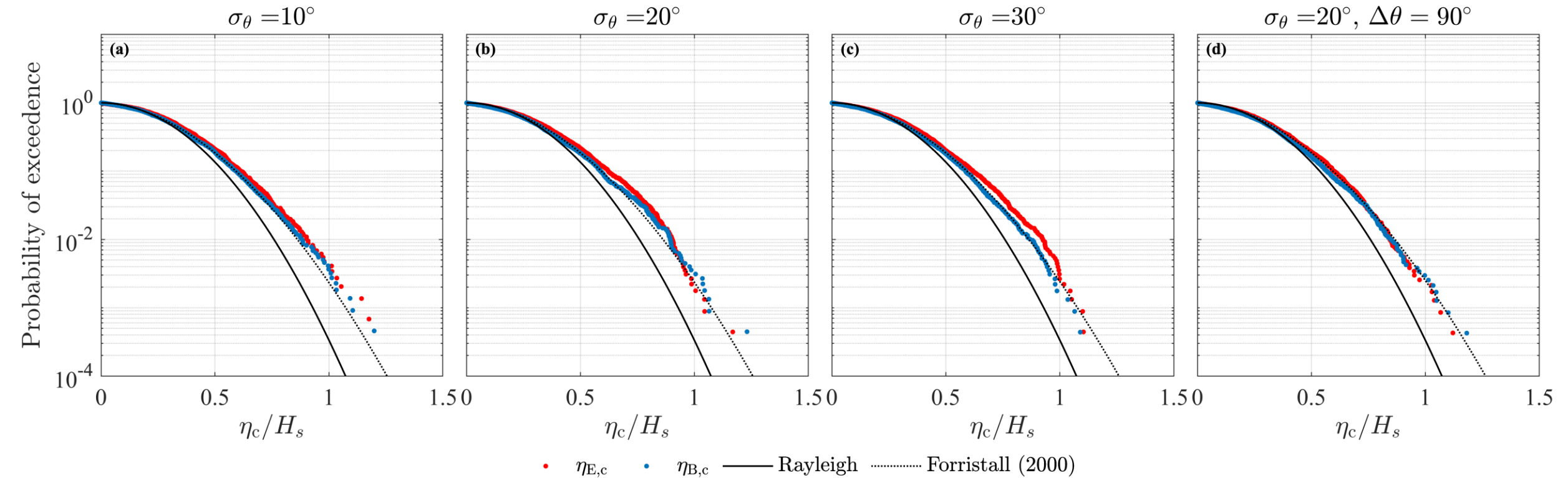
THE UNIVERSITY of EDINBURGH
School of Engineering



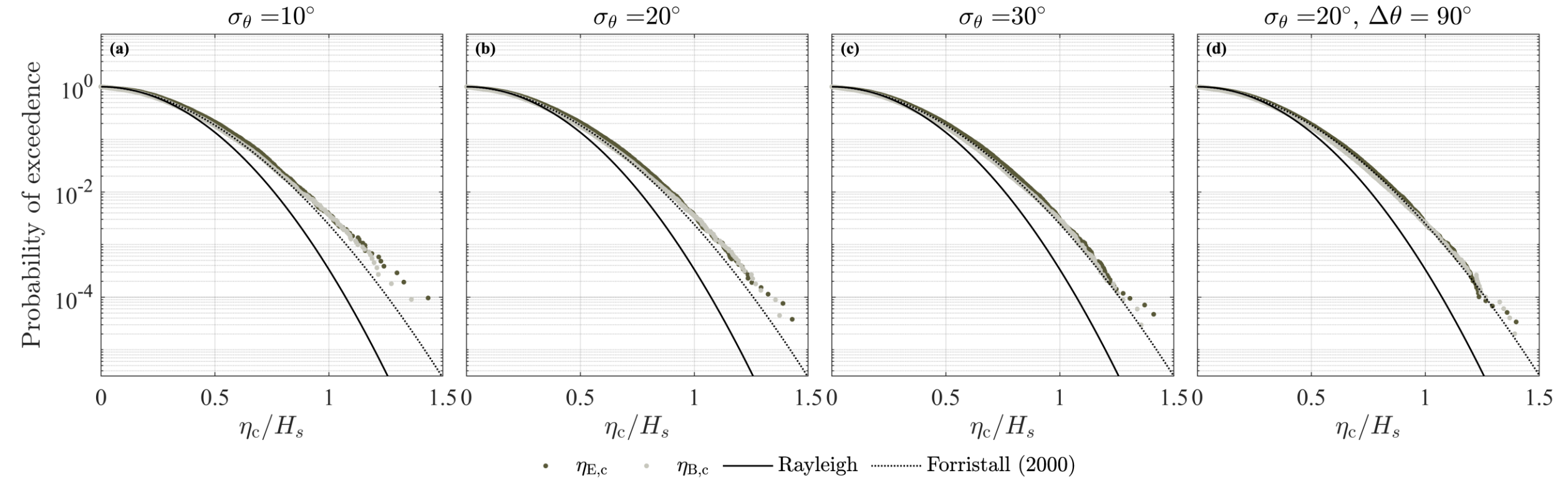
Statistical Properties of Directionally Spread Ocean Waves Measured by Buoys



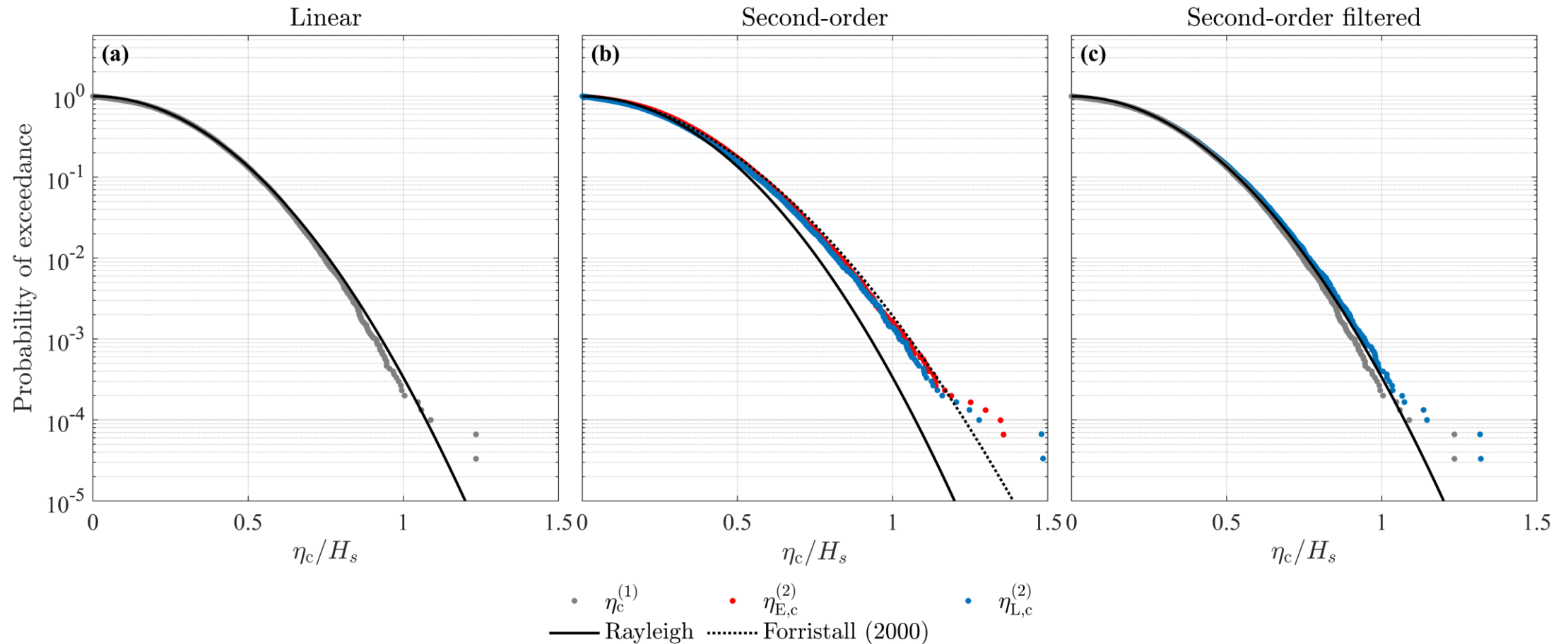
Statistical Properties of Directionally Spread Ocean Waves Measured by Buoys



Statistical Properties of Directionally Spread Ocean Waves Measured by Buoys

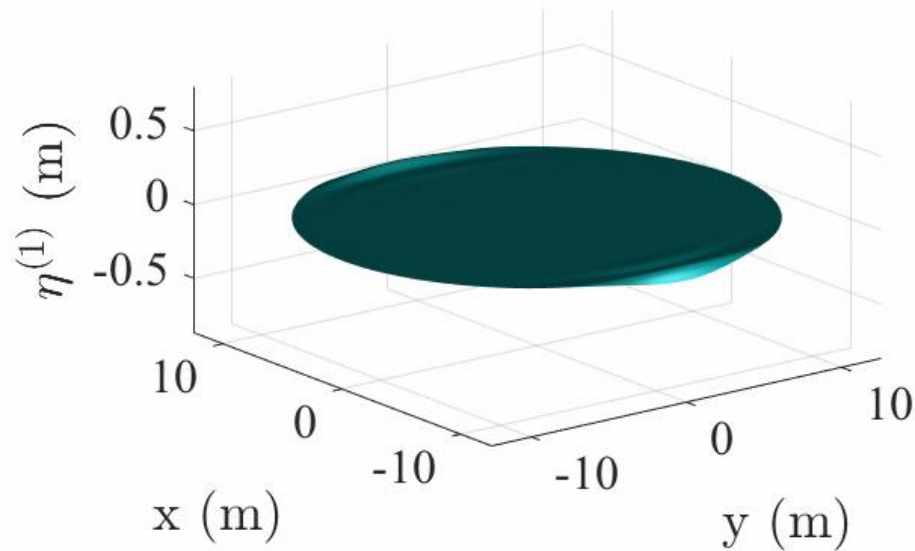


Approximate retrospective correction method for crest heights



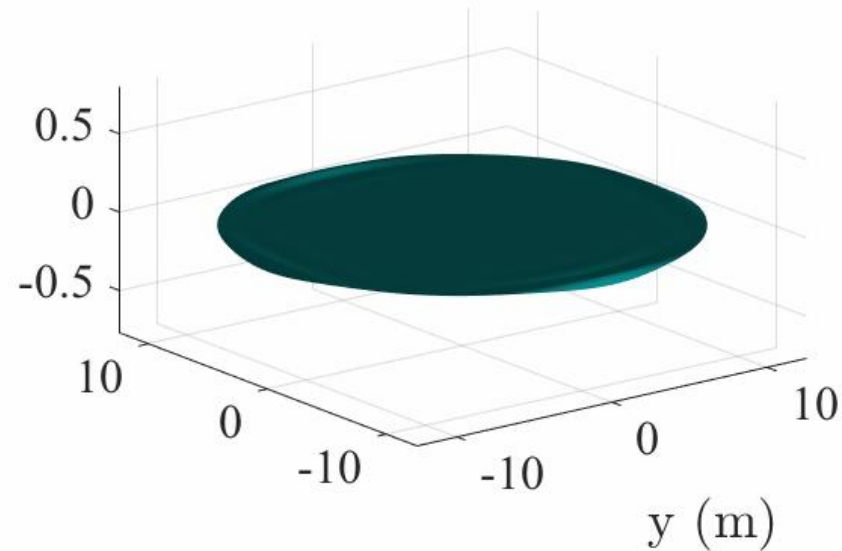
Approximate retrospective correction method for crest heights

$$\sigma_\theta = 10^\circ, \Delta\theta = 0^\circ$$



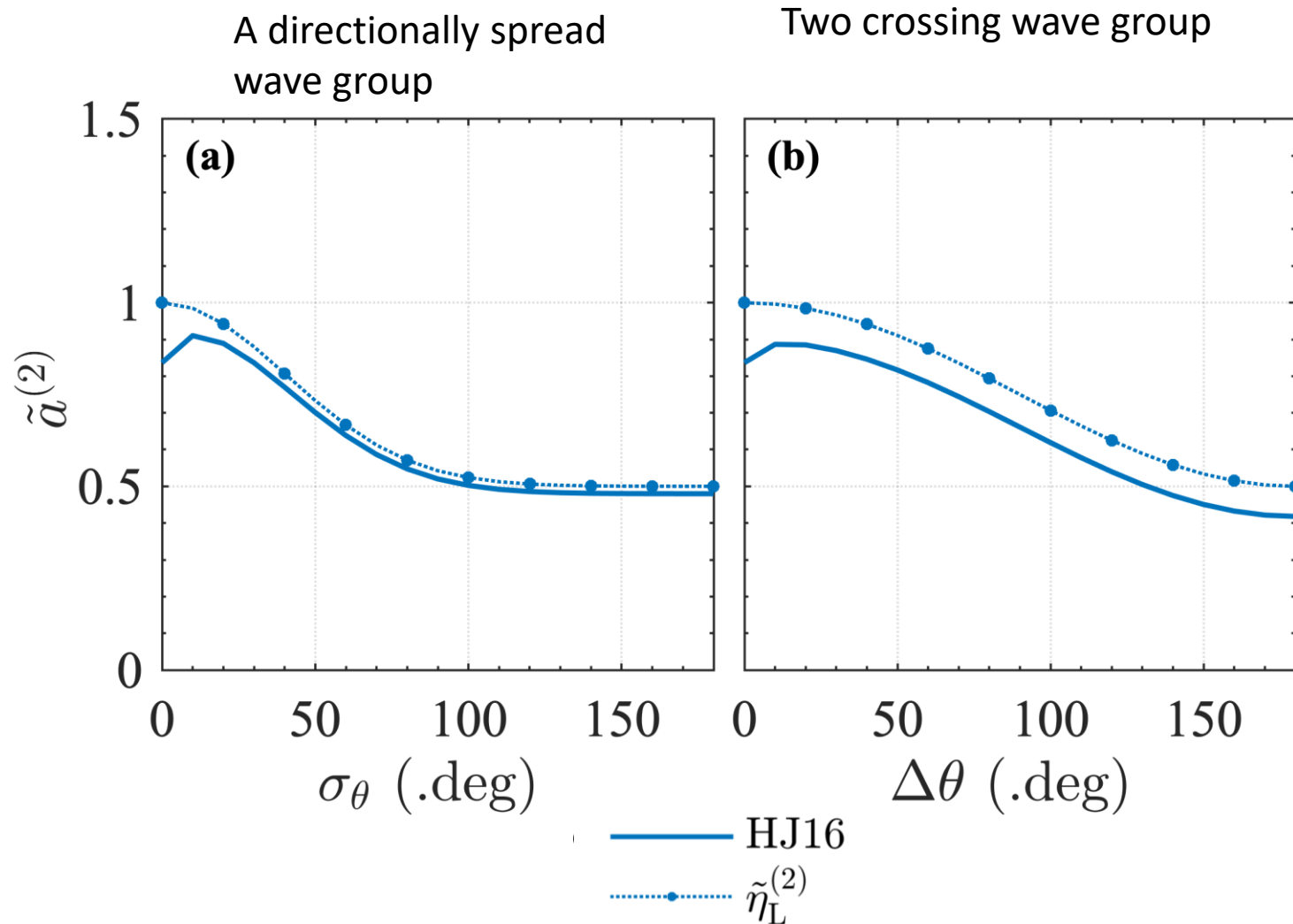
$$\tilde{\eta}^{(2)}(\sigma_\theta) = \frac{1}{2} \left(1 + e^{-\sigma_\theta^2} \right)$$

$$\sigma_\theta = 10^\circ, \Delta\theta = 90^\circ$$



$$\tilde{\eta}^{(2)}(\Delta\theta) = \frac{1}{2} + \frac{1}{4} (1 + \cos(\Delta\theta))$$

Approximate retrospective correction method for crest heights



Approximate retrospective correction method for crest heights

$$\eta_c \approx \eta_c^{(1)}$$

$$\eta_{Corr,c} = \eta_c + \eta_{c-}^{(2)}$$

Approximate retrospective correction method for crest heights

$$\eta_c \approx \eta_c^{(1)}$$

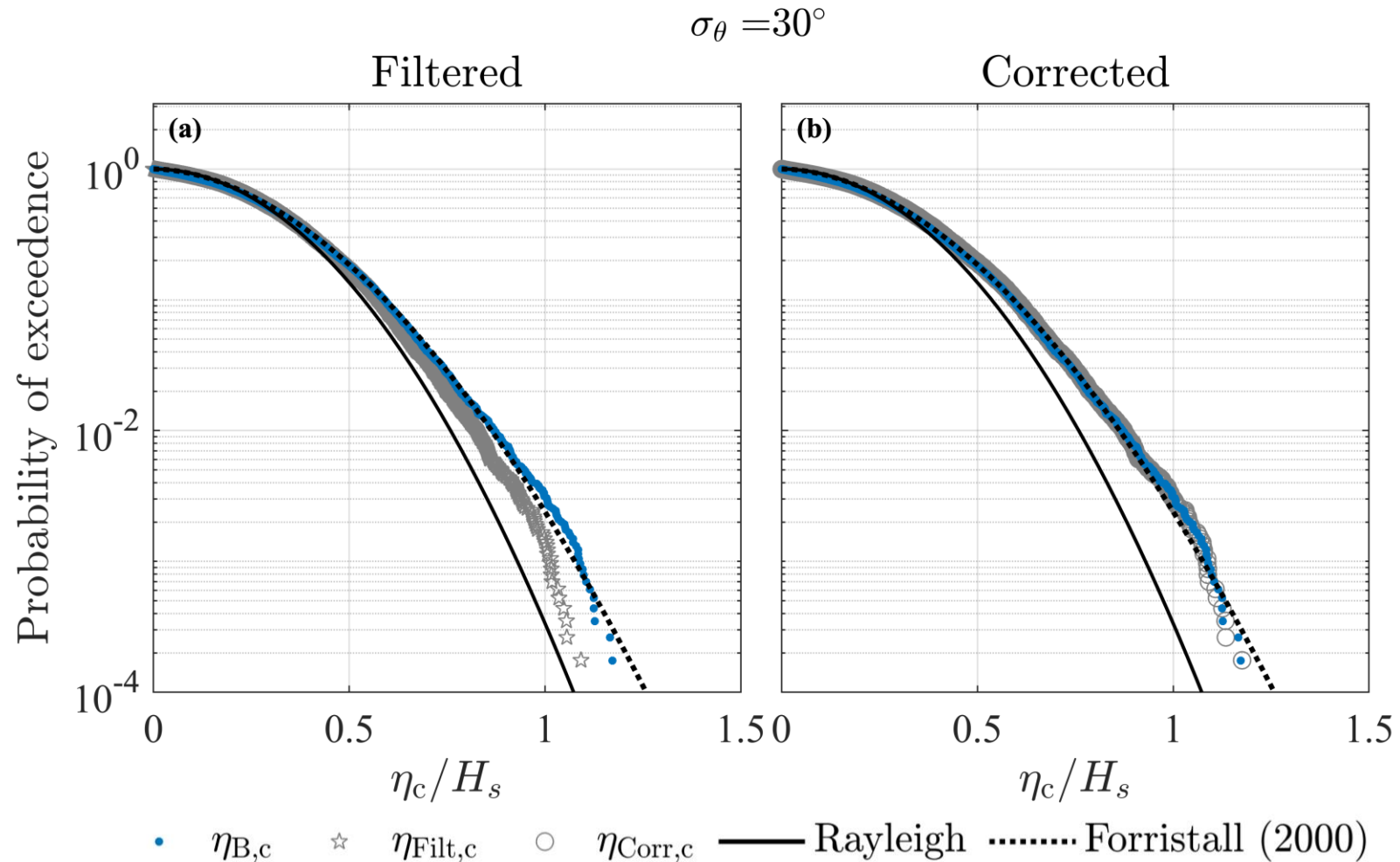
$$\eta_{\text{Corr},c} = \eta_c + \eta_{c-}^{(2)}$$

$$\eta_{c-}^{(2)} = \frac{1}{2}(\eta_c)^2 k_0 \tilde{\eta}^{(2)}(\sigma_\theta, \Delta\theta)(1 - \varepsilon_{\text{hpf}})$$

$$\tilde{\eta}^{(2)}(\sigma_\theta) = \frac{1}{2}(1 + e^{-\sigma_\theta^2})$$

$$\tilde{\eta}^{(2)}(\Delta\theta) = \frac{1}{2} + \frac{1}{4}(1 + \cos(\Delta\theta))$$

Approximate retrospective correction method for crest heights



Conclusions

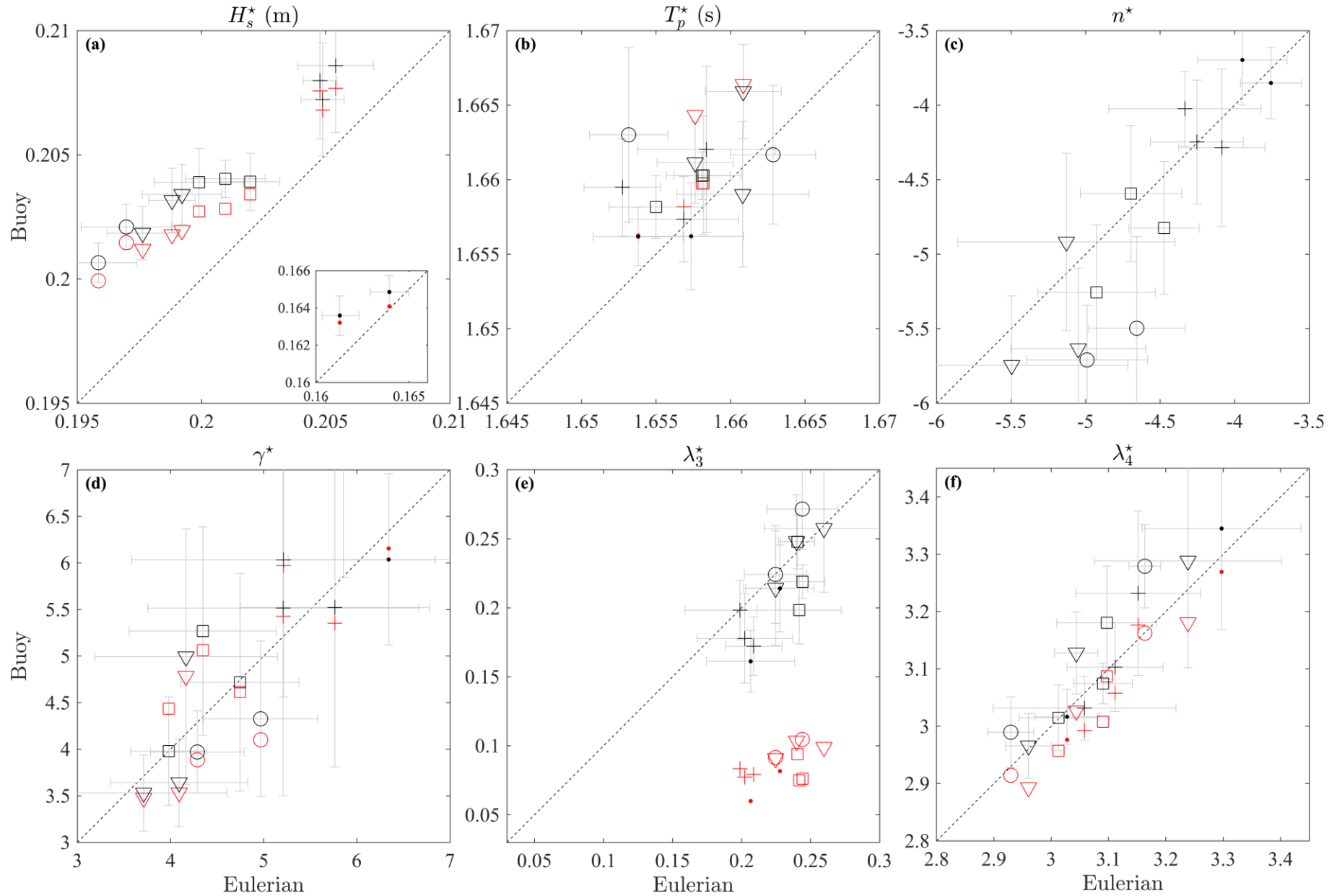
- In deep water (ocean waves), second-order Lagrangian motion causes the cancellation of super-harmonic ($\sigma \theta \rightarrow 0$) and an increase in sub-harmonic contribution to crest height
- $O(2)$ effects alone will not result in a change to crest height, however, this constitutes a shifting of bound energy from low to high
- For deterministic extreme (non breaking) wave groups buoy motion is essentially purely Lagrangian
- Spectral parameters (H_s , T_p . Etc.) are not significantly different between buoys and gauge measurements
- Filtering slightly affects measured H_s , and significantly reduces measured skewness λ^3
- Wave and crest height measured by buoys and gauges follow the same distributions
- Simplified expressions for second-order contribution to crest height can be used to retrospectively correct measurements and remove the effects of filtering
- These experiments do not consider a realistic mooring configuration, however, if a lack of mooring compliance was to cause an underestimation of crests we believe this would also affect measured wave heights

Thanks for your attention!

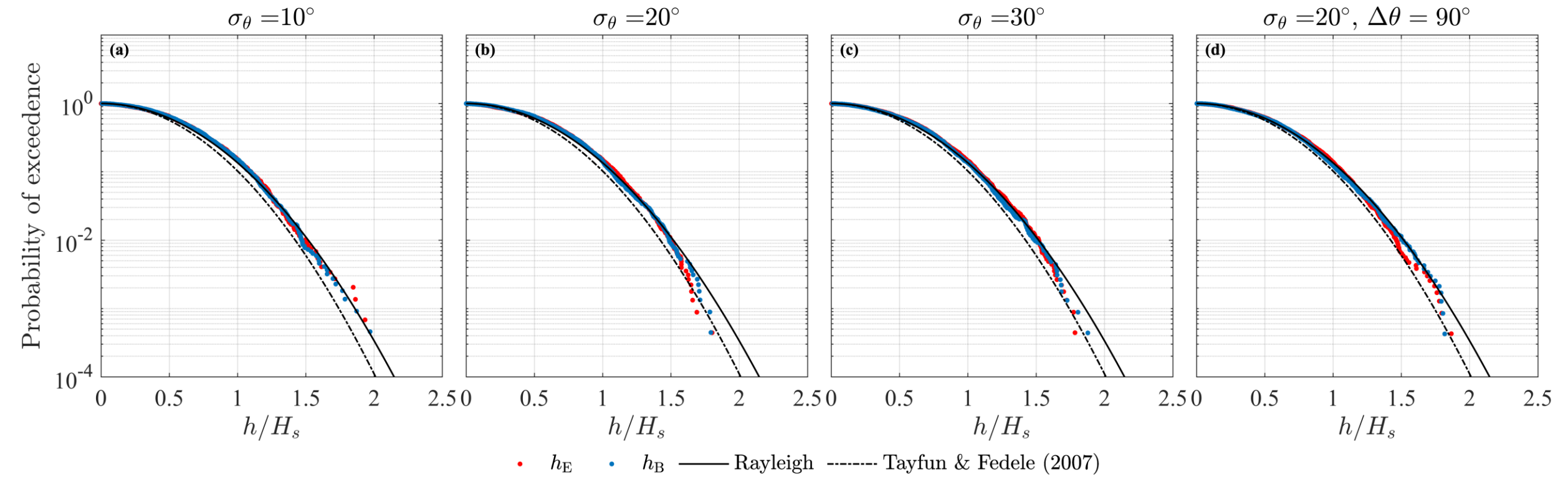
1. M. L. McAllister, and T. S. van den Bremer “Lagrangian Measurement of Steep Directionally Spread Ocean Waves: Second-Order Motion of a Wave-Following Measurement Buoy” **J. Phys. Oceanogr. (in press)**
2. M. L. McAllister, T. S. van den Bremer “Experimental Study of the Statistical Properties of Directionally Spread Ocean Waves Measured by Buoys” **J. Phys. Oceanogr.** (under review)



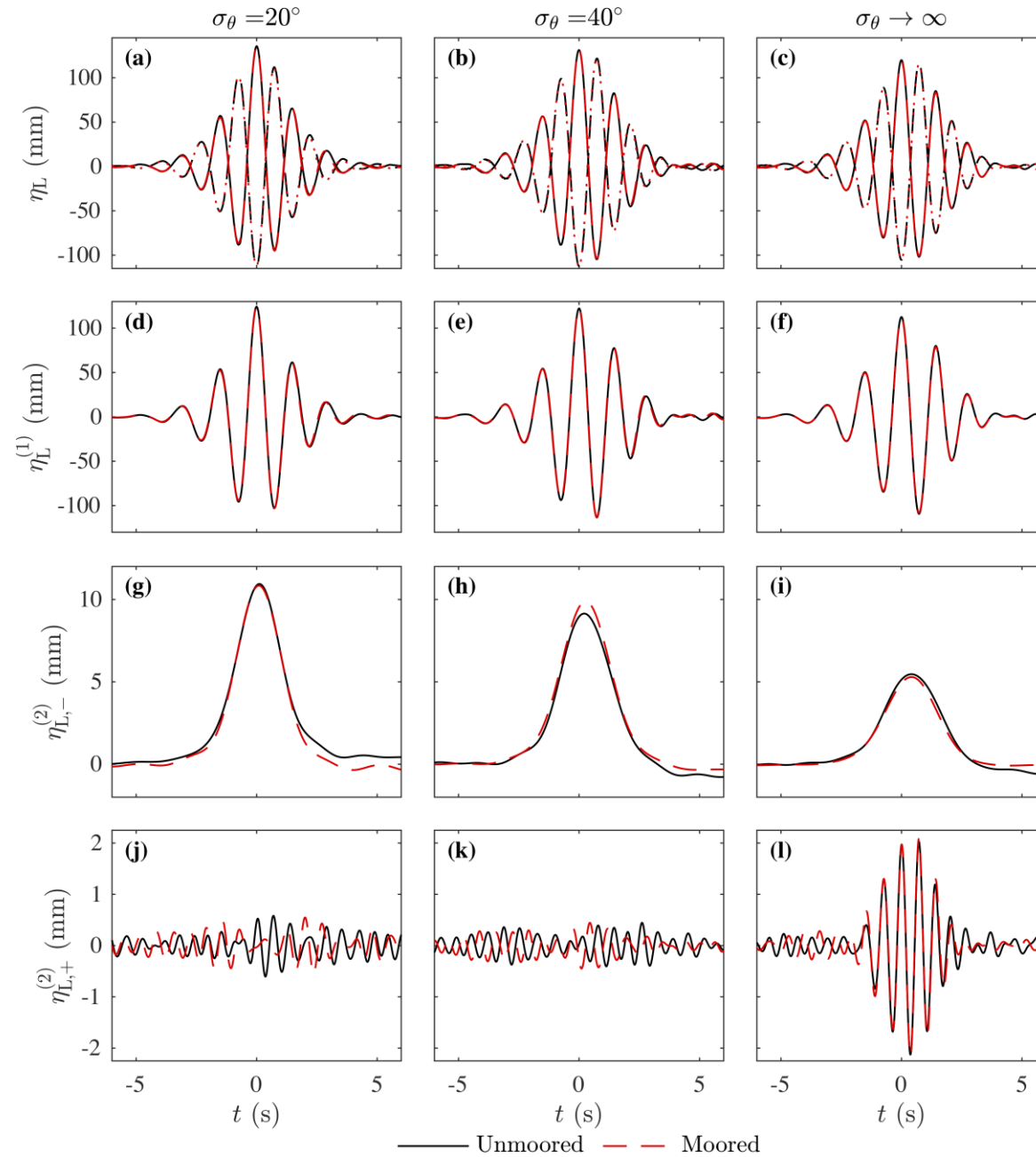
Spectral Parameters



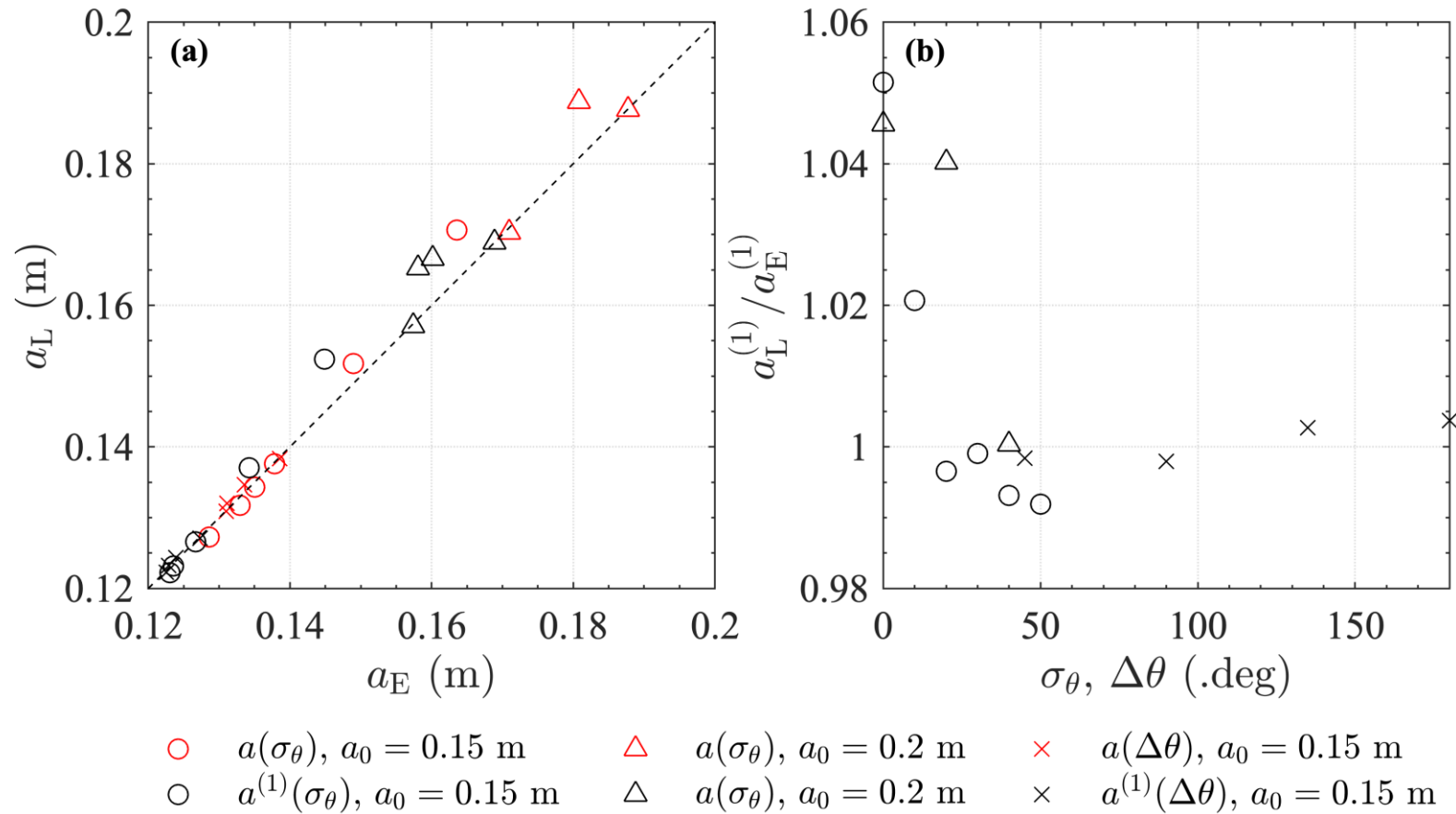
Wave height



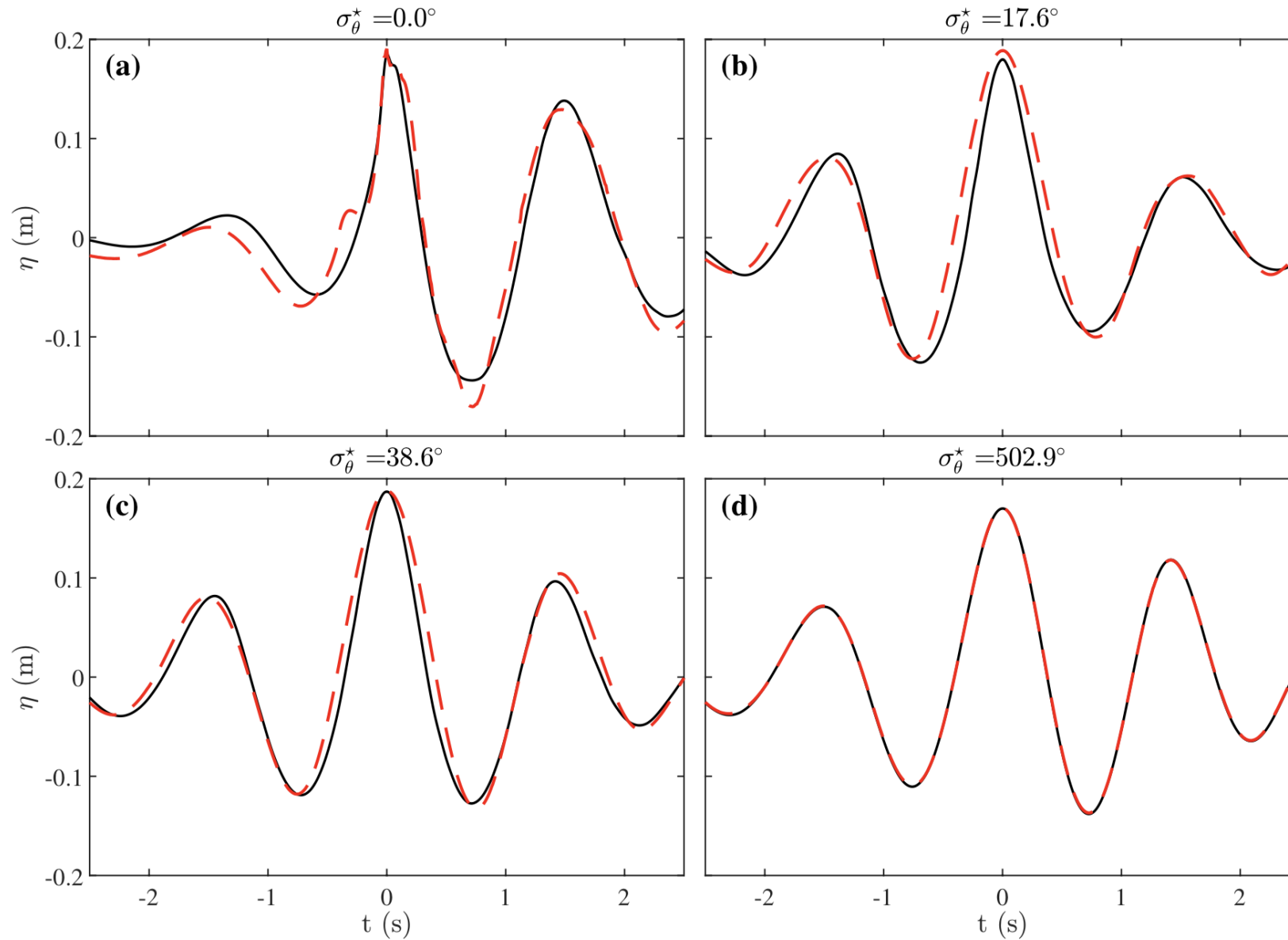
Mooring



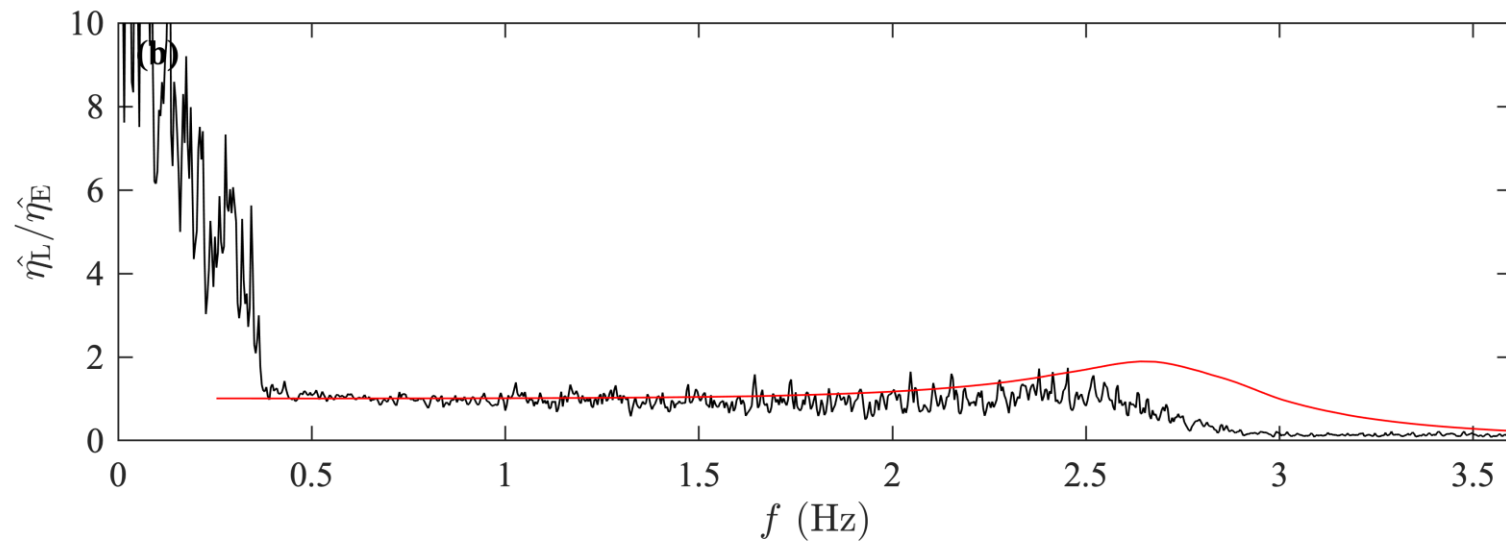
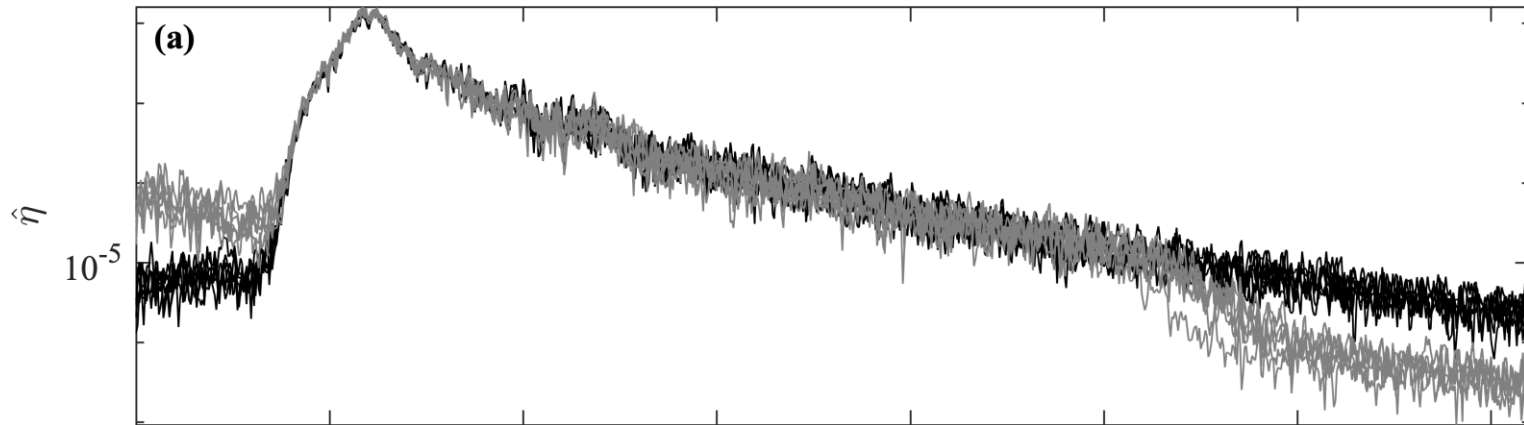
Amplitude/Period



Breaking waves



Frequency attenuation



— Eulerian — Lagrangian — Ballast & Zandbergen (2005)